

# SSPD'03 Conference

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## Solution of Ge containing zeolites by applying direct methods to powder data

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synchrotron radiation

inorganic structures

whole profile fitting

FIPS (Estermann et al.)

refinement function

systematic overlap (Rius, Miravittles, Gies, Amigó)

accidental overlap

**Integrated intensities**

**Refinement of phases**

**Structure completion**

**dominant scatterer:**

automated  $\Delta F$  recycling

lighter ligand atoms not required

**weak dominant scatterers:**

fragment / atom  $\Delta F$  recycling

lighter ligand atoms required

FOCUS (Grosse-Kunstleve et al.)

## The true structure

$$\rho(x) \leftrightarrow \mathbf{E}_H = (E_H, \varphi_H)$$

$$\begin{aligned} \mathbf{E}_H &= 1/N^{1/2} \sum_j \exp i 2\pi H x_j \\ &= E_H \exp i \varphi_H \end{aligned}$$

$$\Phi = \{ \dots, \varphi_H, \dots \}$$

$$E_H^2 = 1 + (1/N) \sum_j \sum_k \cos 2\pi H (x_j - x_k) \quad j \neq k$$

Corrections
L, P, k
f <sub>0</sub> , B, ε <sub>H</sub>
<E> = 1

## The squared structure

$$\rho(x)^2 \leftrightarrow \mathbf{G}_H = (G_H, \psi_H)$$



$$E_H = K G_H$$

$$\psi_h = \varphi_h$$

$$\mathbf{G}_H(\Phi) = \sum_{h'} E_{h'} E_{H-h'} \exp(i(\varphi_{h'} + \varphi_{H-h'}))$$

## $E_H$ in terms of the interatomic vectors

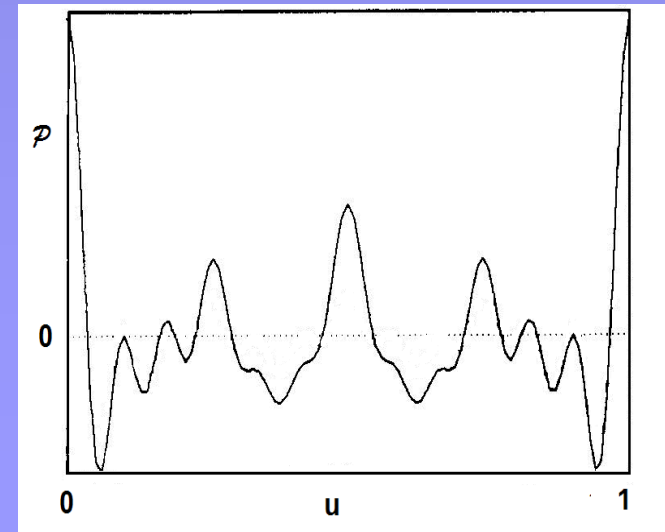
$$E_H \approx 1 + K_H \sum_j \sum_k \cos 2\pi H(x_j - x_k) \quad j \neq k$$

↑  
 $\langle E_H \rangle$

**Modulus and origin syntheses:**

$$P(u) = (1/V) \sum_H E_H \cos 2\pi H u$$

$$U(u) = (1/V) \sum_H \langle E \rangle \cos 2\pi H u$$



## $E_H$ in terms of the phases $F$

$$\begin{aligned} E_H(\Phi) &= K \cdot \{ \exp i\psi_{-H} \cdot \mathbf{G}_H(\Phi) \} \\ &= K \cdot \sum_{h'} E_{h'} E_{H-h'} \cos(\psi_{-H} + \varphi_{h'} + \varphi_{H-h'}) \end{aligned}$$

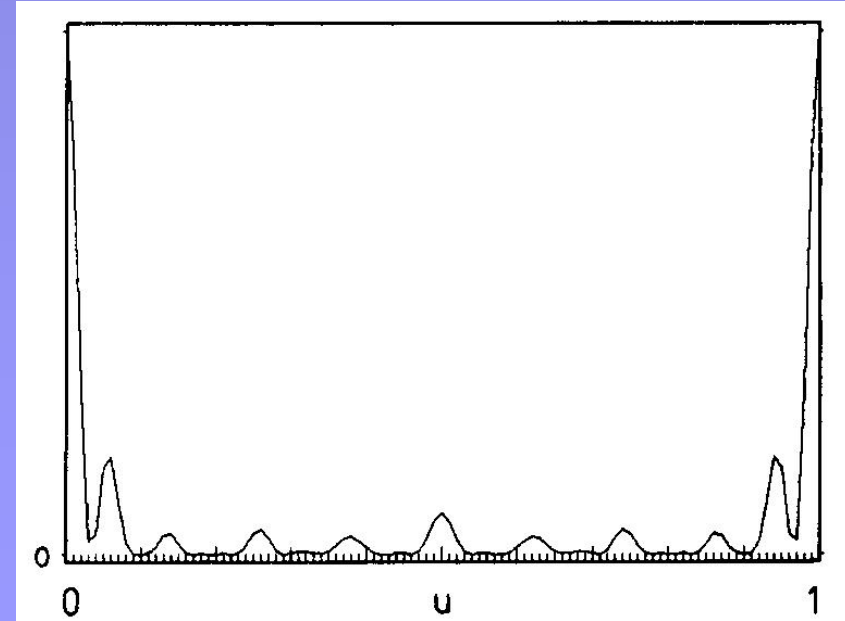
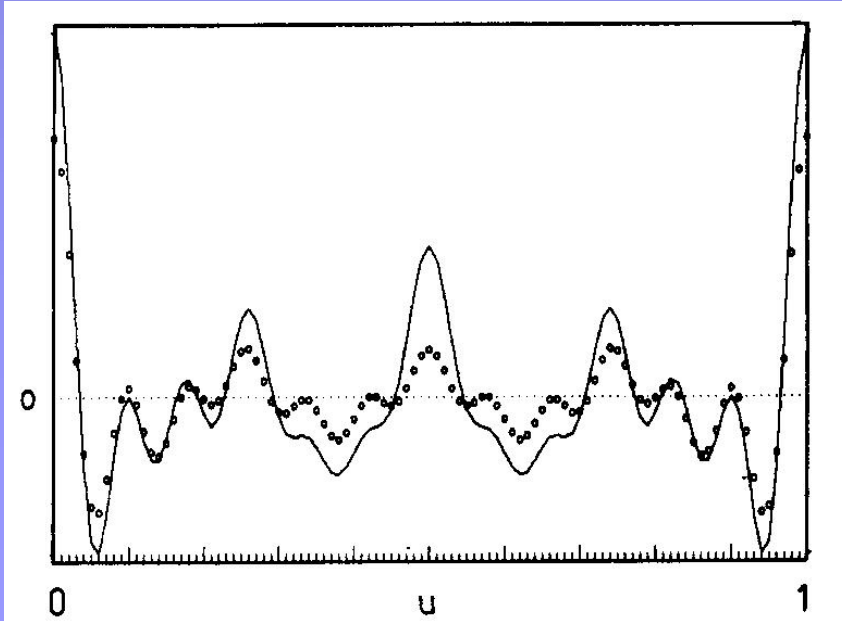
## Calculated modulus synthesis:

$$P(u, \Phi) = (1/V) \sum_H E_H(\Phi) \cos 2\pi H u$$

## The modulus sum function

$$Z(\Phi) = V^2 \int_V P(u) P(u, \Phi) du = \max!$$

$$Z(\Phi) = K \sum_H E_H E_H(\Phi) = \max!$$



## The modulus sum function

$$Z(\Phi) = K \sum_H E_H \sum_{h'} E_{h'} E_{H-h'} \cos(\psi_{-H} + \varphi_{h'} + \varphi_{H-h'})$$

- Only the **large E's** are significant.
- For the large reflections **h** it holds  $\psi = \varphi$
- Phase refinement with **Z** often leads to overconsistent triplets, i.e. for most triplets

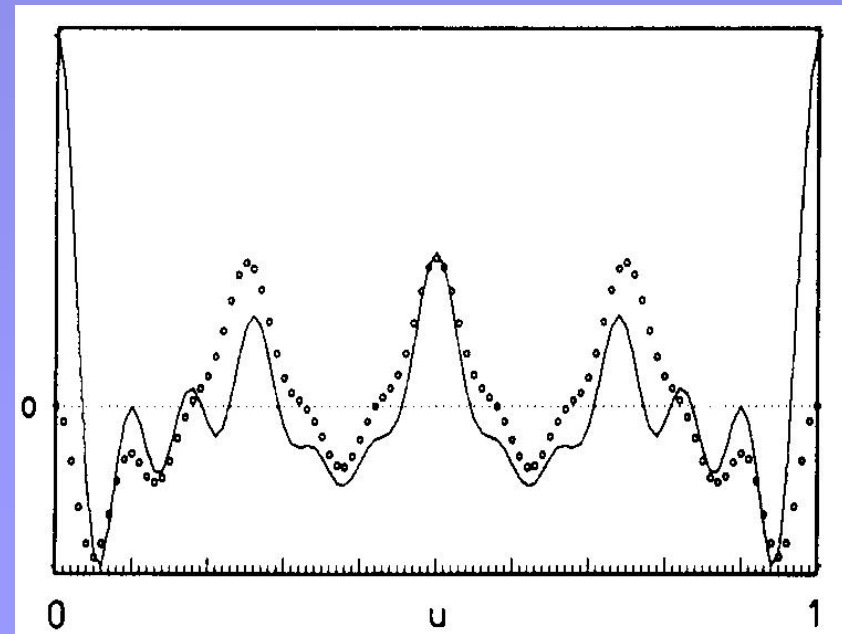
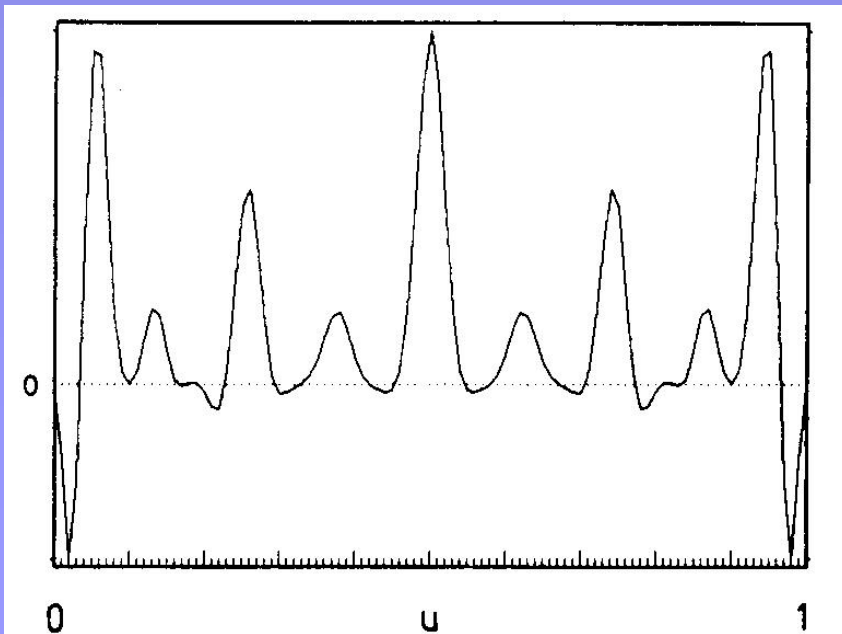
$$\varphi_{-h} + \varphi_{h'} + \varphi_{h-h'} \approx 0^\circ \quad (\mathbf{U \text{ atom solution}})$$



## The constrained modulus sum function

$$S(\Phi) = Z(\Phi) - V^2 \int_V U(u) U(u, \Phi) du = \max!$$

$$S(\Phi) = K \sum_H (E_H - \langle E \rangle) E_H(\Phi) = \max!$$



## Computation of S(F)

$$\begin{aligned} S(\Phi) = & K \sum_h \sum_{h'} E_{-h} E_{h'} E_{h-h'} \\ & \times [3 - \langle E \rangle (1/E_{-h} + 1/E_{h'} + 1/E_{h-h'})] / 3 \\ & \times \cos(\varphi_{-h} + \varphi_{h'} + \varphi_{h-h'}) \\ & + K \sum_l \sum_h (E_l - \langle E \rangle) E_{-h} E_{h-l} \\ & \times \cos(\psi_l + \varphi_{-h} + \varphi_{h-l}) = \max! \end{aligned}$$



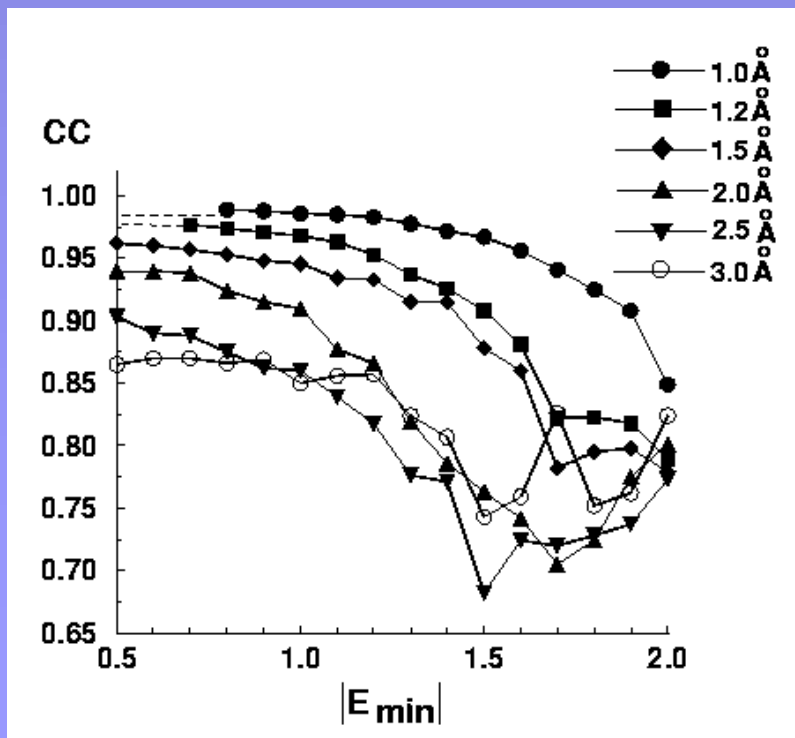
function of  $\Phi_{\text{old}}$

# The $E(h)$ parameters of $S(\Phi)$

$E_{lim}$  = minimum large  $E(h)$  (1.45-1.25)

$d_{min}$  = minimum  $d$  value  $\Leftrightarrow$  atom types

$E_{ratio}$  =  $N_l/N_h$  fixes the number of weak  $E(l)$



J.Rius, X.Torrelles,  
C.Miravittles, J.M.Amigó,  
M.M.Reventós Acta Cryst. (2002)  
A58 21-26.

## Positive triplets

$$Z(\Phi) = K \sum_H \sum_{h'} E_H E_{h'} E_{H-h'} \cos(\psi_{-H} + \varphi_{h'} + \varphi_{H-h'})$$

# Positive and negative quartets

$$Q(\Phi) = 2/N \sum_H \sum_K \sum_L E_H E_K E_L E_{H-K-L}$$

$$\times (E_{-H+K}^2 + E_{-H+L}^2 + E_{K+L}^2 - 3)$$

$$\times \cos(\varphi_{-H} + \varphi_K + \varphi_L + \varphi_{H-K-L}) = \max!$$

Schenk (1974); Hauptman (1974); Giacovazzo (1976)

$$\int_V P'(u) P(u, \Phi) du$$

Rius et al. (1997)

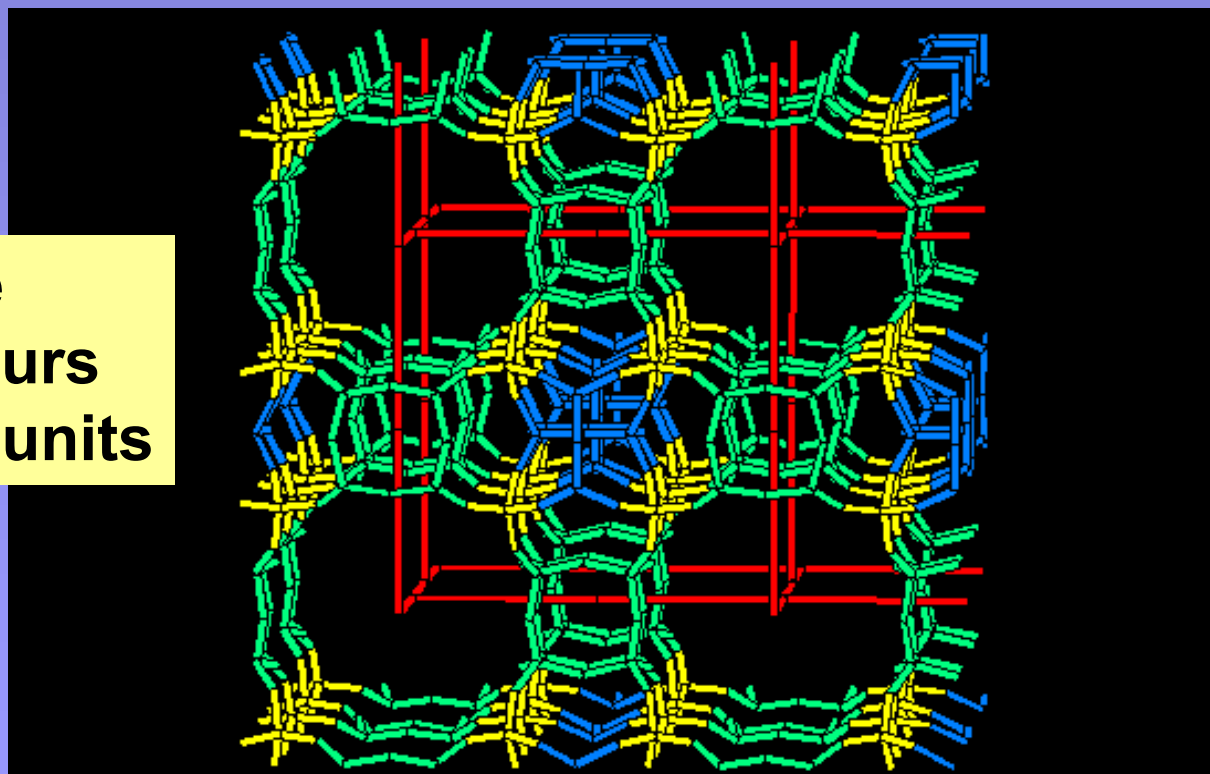
$$\int_V P'(u) P(u, \Phi) du$$

Rius (1993)

# Framework Isomorphous Substitution as a Structure-Directing Mechanism



**F and Ge in the  
synthesis gel favours  
formation of D4MR units**



**Polymorph C of beta (ITQ17)**

## Basic building unit of D4MR family

ITQ-17:  $a + a$

BEC

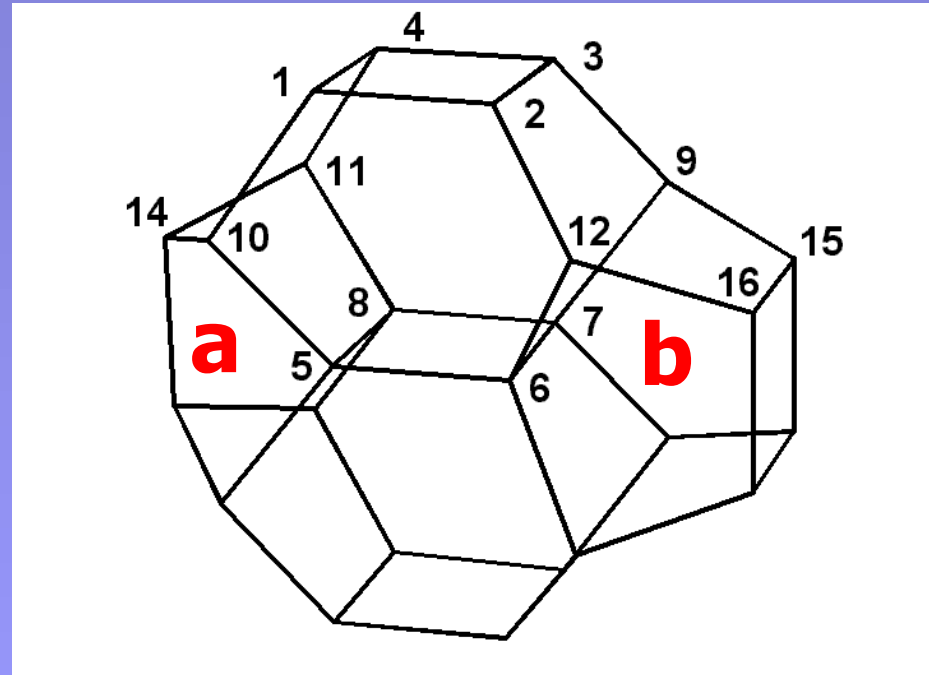
ITQ-7:  $a + a$

ISV

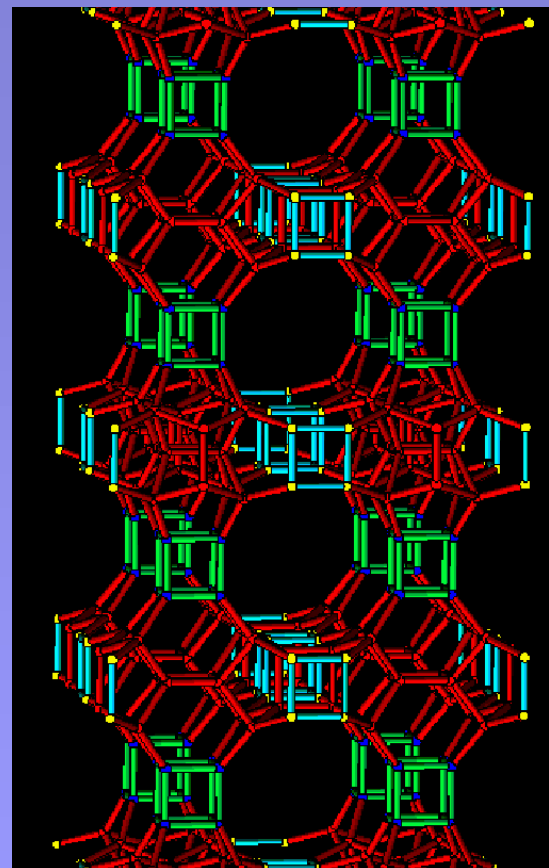
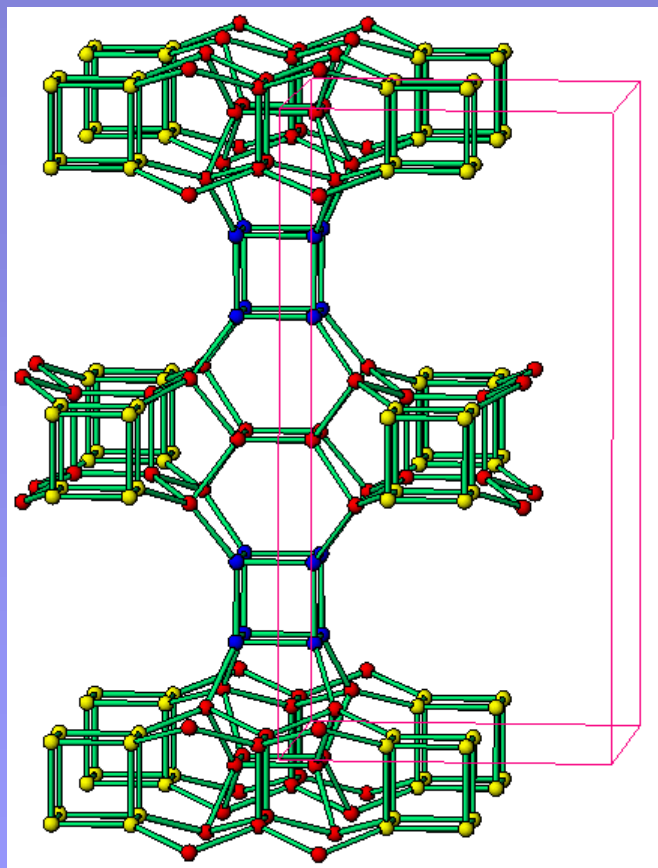
ITQ-22:  $a + b$

IWW

ITQ-24:  $b + b$



## Basic building unit of ITQ-7



L.Villaescusa, P.Barrett, M. Cambor

*Angew. Chem. Int. Ed.* 1999, 38, 1997-2000



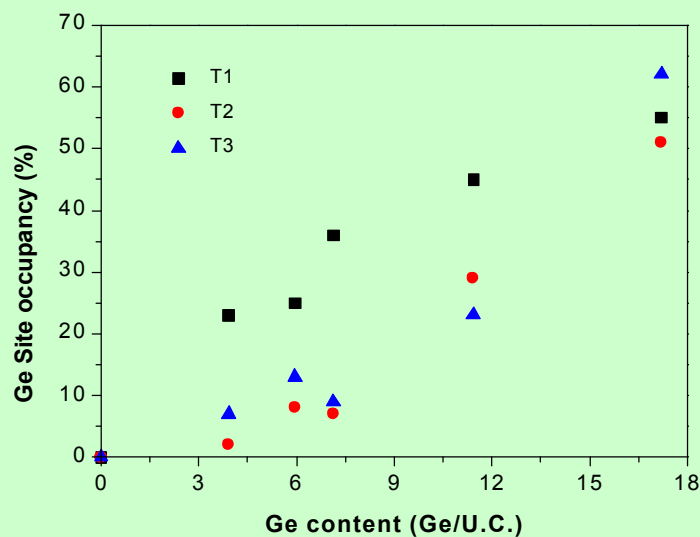
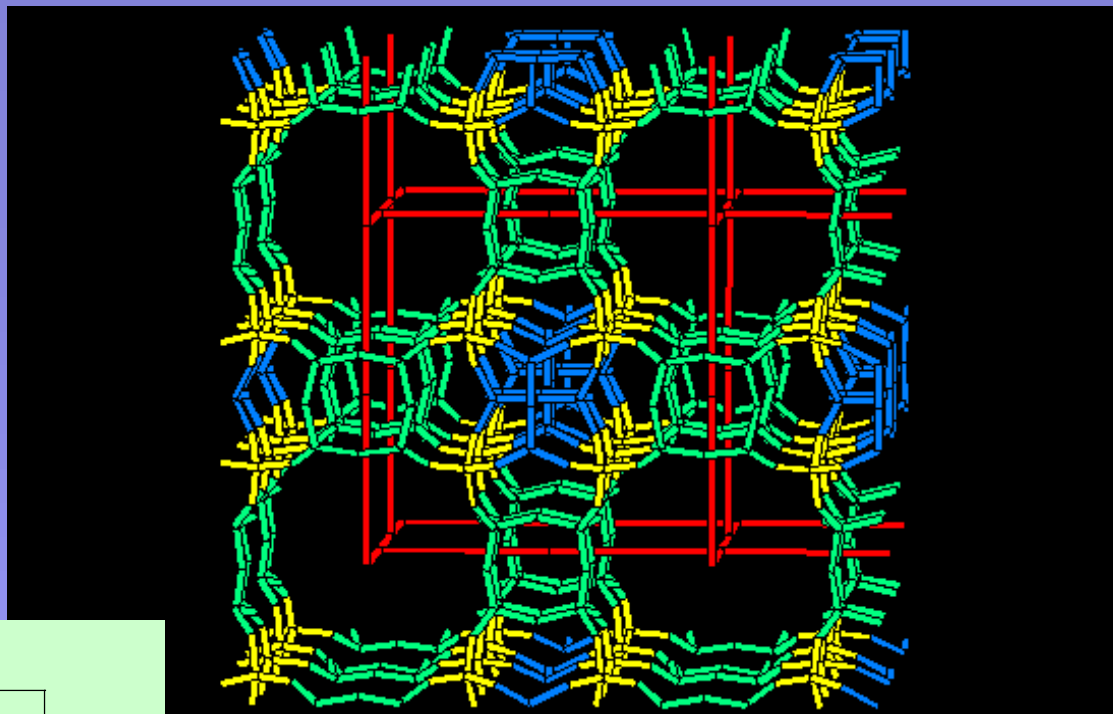
# Ge distribution over the T sites in ITQ-17

Si:Ge = 1.8

T1: 0.46 Ge

T2: 0.28 Ge

T3: 0.23 Ge



A.Corma, M.Navarro, F.Rey, J.Rius,  
S.Valencia *Angew. Chem. Int. Ed.*  
2001, 40, 2277-2280



# ITQ22- Preliminary Data



## Crystal data:

**a= 42.14424 Å**

**b= 12.99000 Å**

**c= 12.68428 Å**

**orthorhombic**

**V= 6944.1 Å<sup>3</sup>**

**Space group: Pbam (55)**

**r (a.s.) = 2.22 g/cm<sup>3</sup>**

**r (calcined) = 1.87 g/cm<sup>3</sup>**

## Composition:

**10.35359% C**

**1.84144% H**

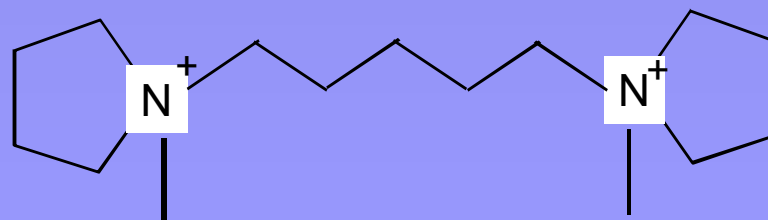
**1.4816% N**

**Si/Ge=3.25**

**wt. loss 15.58%**

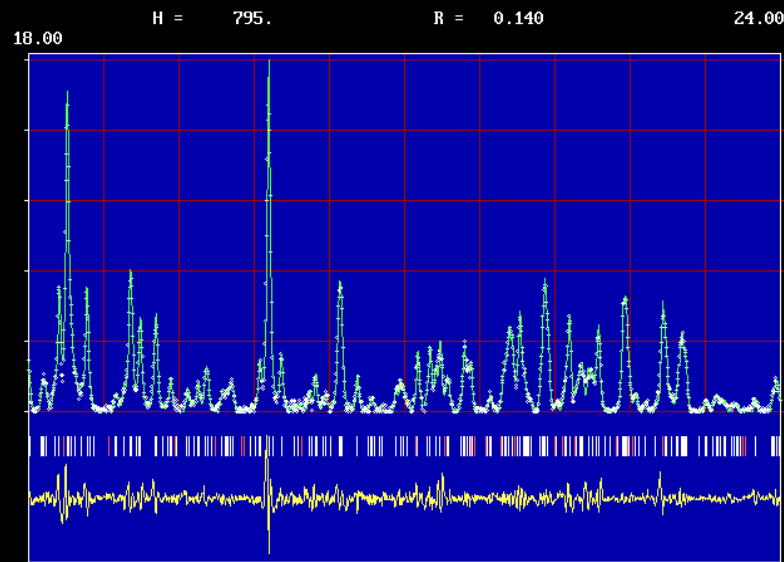
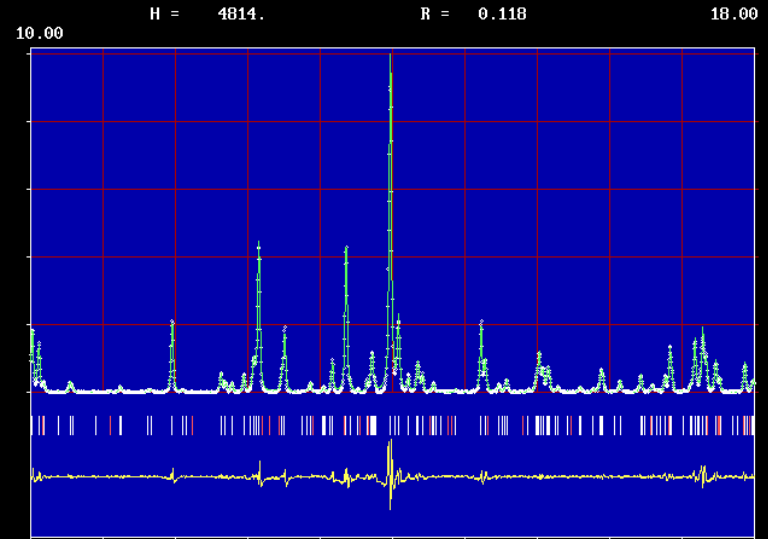
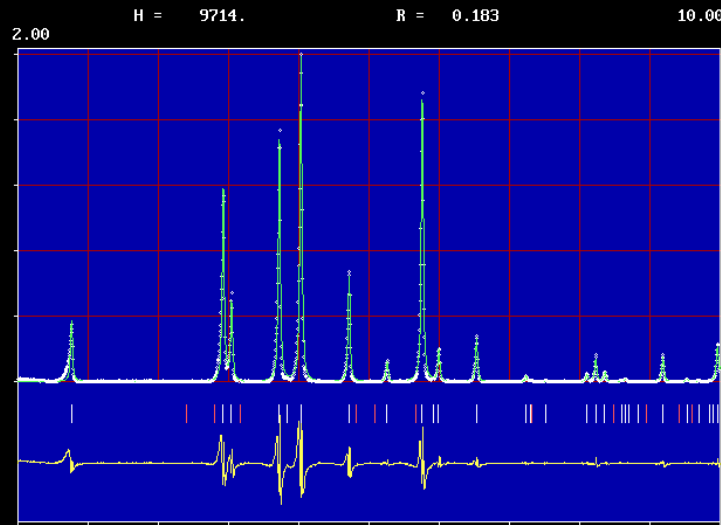
**110.8 TO<sub>2</sub>/unit cell**

**4.9 template /unit cell**



**1,5-bis(metilpirrolidinium)-pentane [C<sub>15</sub> H<sub>32</sub> N<sub>2</sub>]<sup>2+</sup>**

# Whole-pattern fit without structure model of ITQ22



Line DW22 at LURE

$\lambda = 0.9611 \text{ \AA}$

( $\varnothing = 1 \text{ mm}$ )



# Summary of intensity extraction

## Method:

1. Whole pattern profile fitting by fixed point iteration → **profile parameters**
2. Intensity extraction by L.S. profile fitting of regions → **intensities + e.s.d.'s**

**363** intensities for  $d \geq 2.24\text{\AA}$

from which **49** overlapped within  $2.58 - 2.24\text{\AA}$



## ITQ22: Summary of direct methods (1)

N.shell	$d_{inf}$	$\Sigma F_c^2 / \Sigma F^2$	N. ref	$\langle F^2 \rangle$
1	3.83	1.03	225	15285
2	3.04	1.00	217	8986
3	2.66	1.08	247	5801
4	2.41	0.72	164	6446
5	2.24	1.25	153	2829

Wilson plot

SK=0.68      B= 14 Å<sup>2</sup>       $\langle |E^2-1| \rangle = 0.95$  **(0.97)**

## ITQ22: Summary of direct methods (2)



### Control parameters:

**Elim = 1.46**

**47 large E's (3.37-1.46)**

**Eratio = 0.85**



**40 small E's (0.02-0.13)**

**dmin = 2.24Å**

**$\langle E \rangle_{\text{large+small}} = 1.19$**

**solved in Pba2**

Phase refinement with S-TF (**100 sets, 20 cycles**) followed by automated  $\Delta F$  recycling for each solution gives as best solution the one with the highest  $S / S_{\text{exp}}$

**Best solution:  $S / S_{\text{exp}} = 0.826$   $R_{\text{DF}}(\%) = 55.2^*$**

$$R = 1000 \times \left\{ 1 - \frac{[\sum(F_o \cdot F_c)^{1/2}]^2}{\sum F_o \sum F_c} \right\}$$

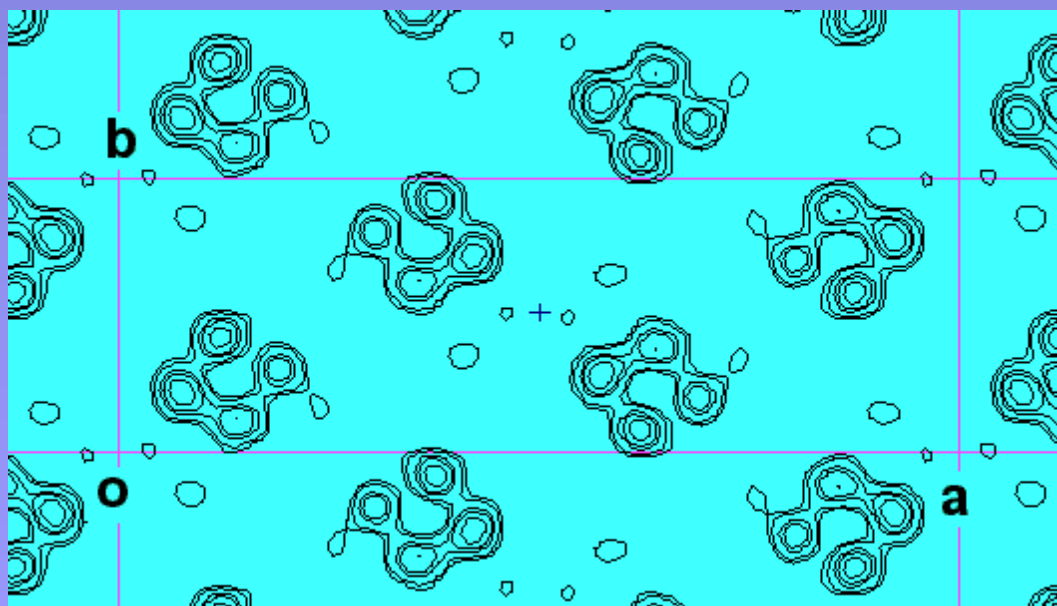
# ITQ22: 3D-imaging at 2.24 Å resolution



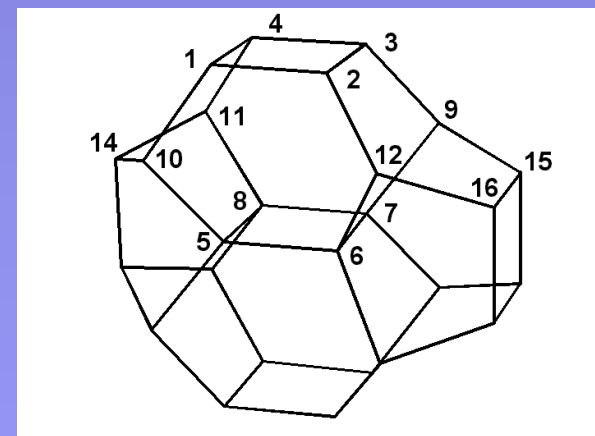
S-TF + automated  
DF refinement



D4MR units + 7 T  
atoms showed up



$a = 42.090$      $b = 12.990$  Å



# Structure completion of ITQ-22: (1)



From the automated Fourier recycling with initial phases from direct methods:

**T1 to T4 + T5 to T8 + T9 to T11**

From the restrained L.S. refinement with fixed occupations for T atoms and 50% Ge at T1-T4 + subsequent DF:

**T12**

**T-T= 3.15(5)Å**

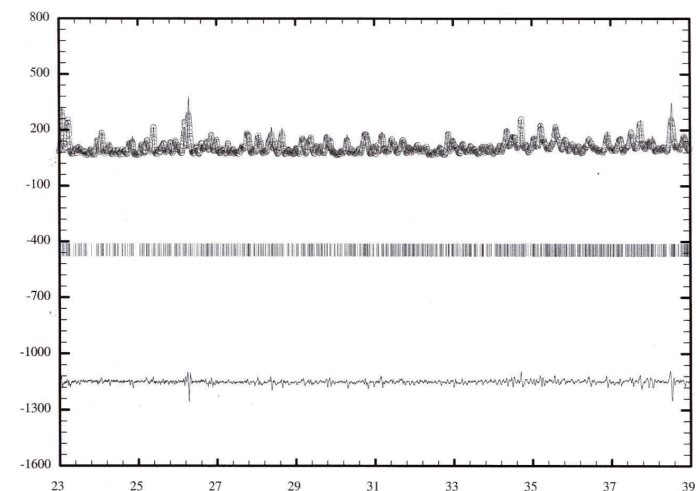
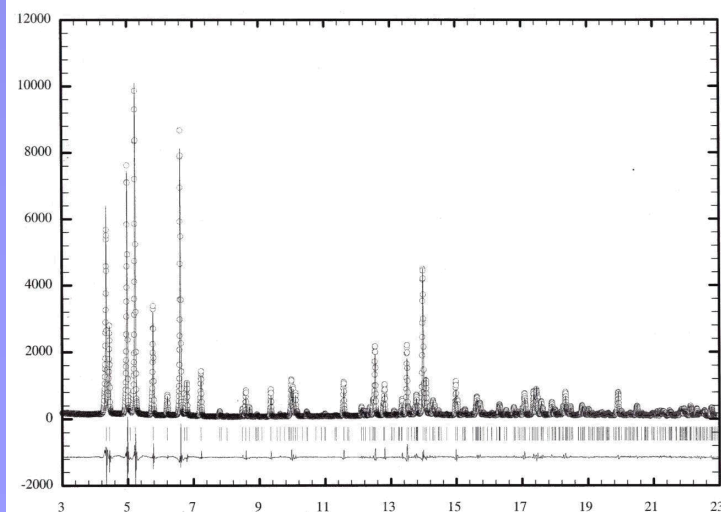


# Structure completion of ITQ-22: (2)

- Restrained L.S. with all T occupations fixed except for T1-T4 +  $\Delta F$   $\Rightarrow$  T13-T16

- L.S. with no restraints for T13-T16

<i>d</i> (Å)	2.24	2.35	2.44	2.54	2.70	2.87	3.09	3.42	4.03	5.26	inf
Nref	40.	36.	35.	37.	34.	35.	41.	32.	36.	37.	
R1	<b>0.582</b>	<b>0.532</b>	<b>0.399</b>	<b>0.402</b>	0.332	0.342	0.256	0.261	0.175	0.148	



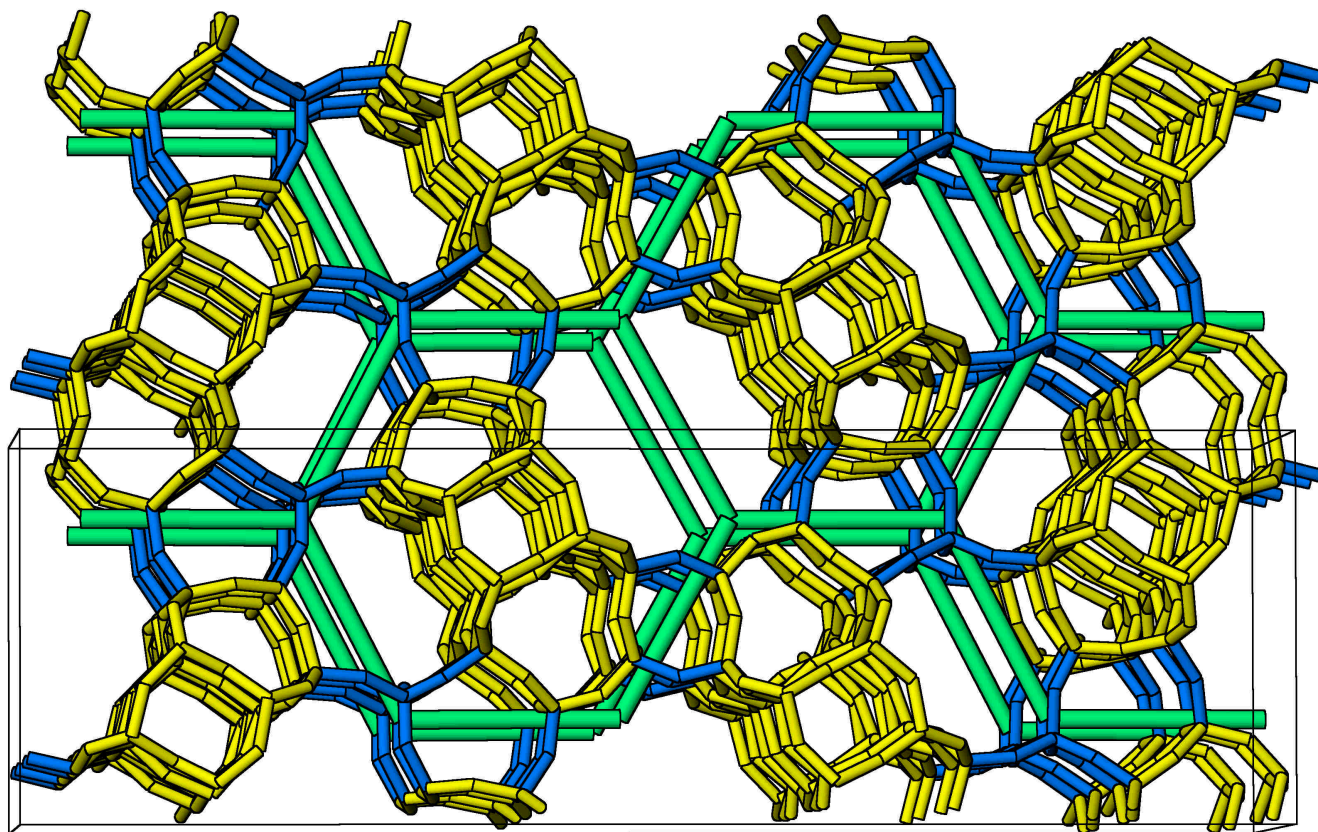
## Fractional atomic coordinates of ITQ-22 (Si:Ge = 4:1)

Atom/ site	x	y	z	site multiplicity	%Ge <sup>[d]</sup>
T1	0.38500	0.9154	0.1275	1	62(3)
T2	0.42261	0.6981	0.1277	1	58(3)
T3	0.35640	0.5802	0.1250	1	48(3)
T4	0.31888	0.7891	0.1225	1	58(3)
T5	0.38387	0.8951	1/2	1/2	0
T6	0.41980	0.6952	1/2	1/2	0
T7	0.35708	0.5625	1/2	1/2	0
T8	0.31899	0.7708	1/2	1/2	0
T9	0.35057	0.4197	0.2980	1	0
T10	0.37882	1.0563	0.3157	1	9(2)
T11	0.27961	0.8590	0.3139	1	9(2)
T12	0.46315	0.6216	0.3125	1	10(2)
T13	0.28922	0.3018	0.3767	1	0
T14	0.30739	1.0734	0.3764	1	11(2)
T15	0.40442	0.2755	0.3769	1	8(2)
T16	0.46674	0.3964	0.3765	1	5(1)

**A.Corma, F.Rey, S.Valencia, J.L. Jordá, J.Rius**

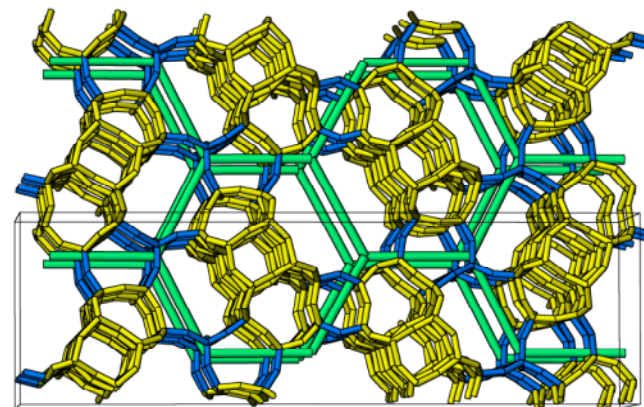
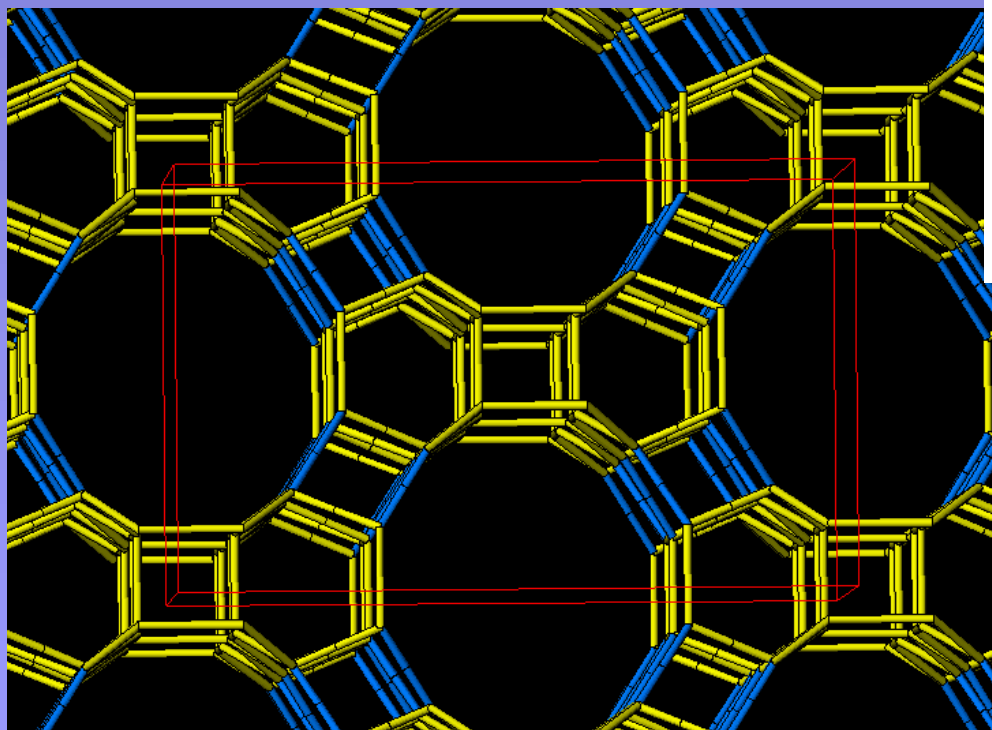
***Nature Materials* 2003, 2, 493-497**

# Upper view of ITQ-22



## ITQ-22

### Upper view of ITQ-24

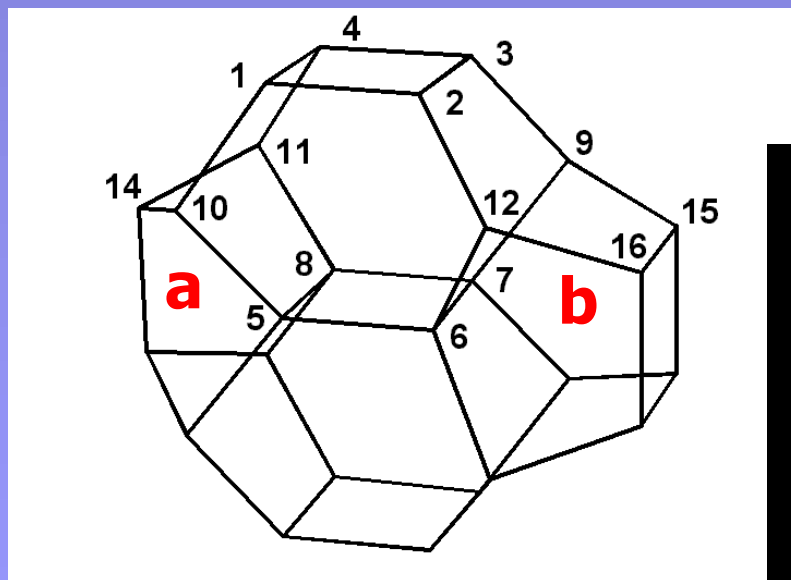


R.Castañeda, A.Corma, V.Fornés, F.Rey & J.Rius JACS (2003)

# BASIC BUILDING UNITS OF D4MR FAMILY

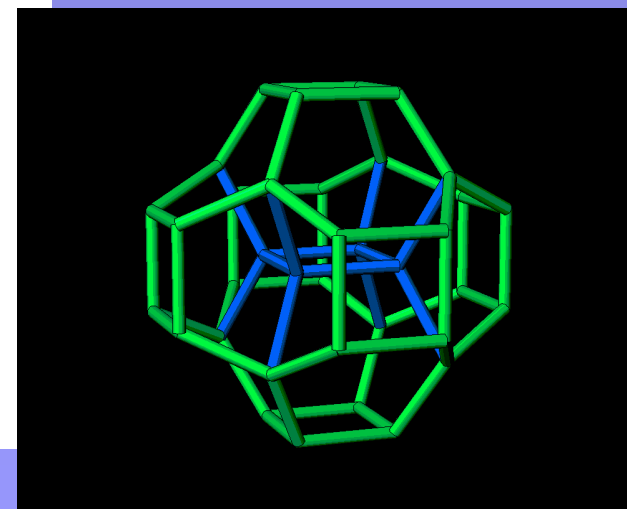
ITQ-17, ITQ-7

$a + a$



ITQ-22

$a + b$



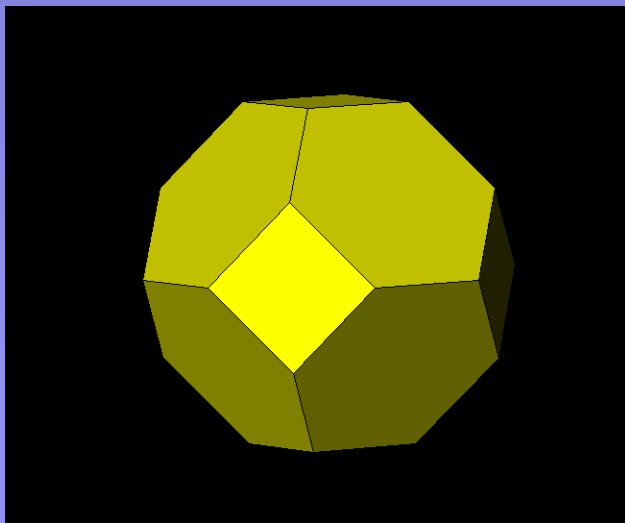
ITQ-24

$b + b$

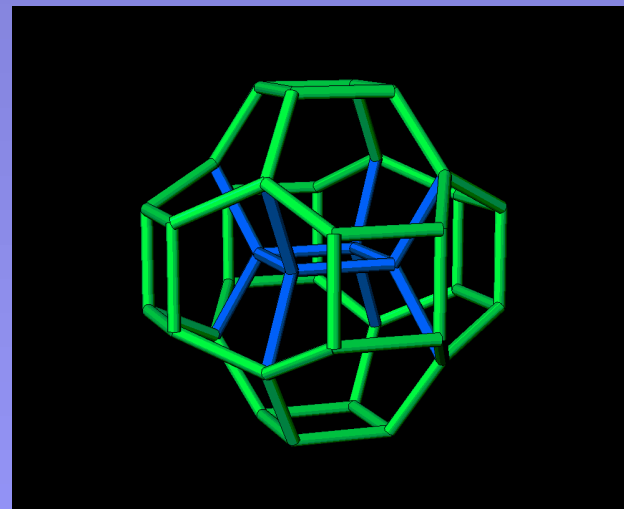
ITQ-21  $4b$



## The building units



sodalite



ITQ-21



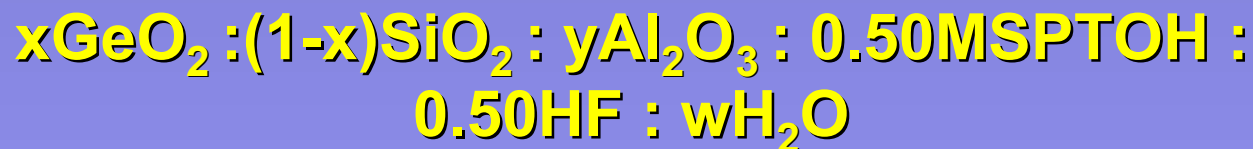
## Basic features of some cubic zeolites

Zeolite	N. of T atoms	Window size	N. of windows	Cavity size
Sodalite	4	2.6	6	~ 9.0
Zeolite A	8	4.1	6	11.4
Faujasite	12	7.4	4	11.8



## Synthesis of ITQ-21

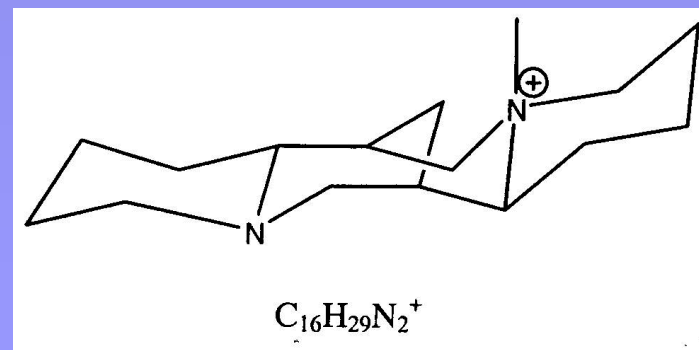
Under hydrothermal conditions at 175°C for 3 days from gels of compositions:



$$x = 0.33 \quad y = 0.00 \quad w = 20$$

$$(x = 0.09 \quad y = 0.02 \quad w = 3)$$

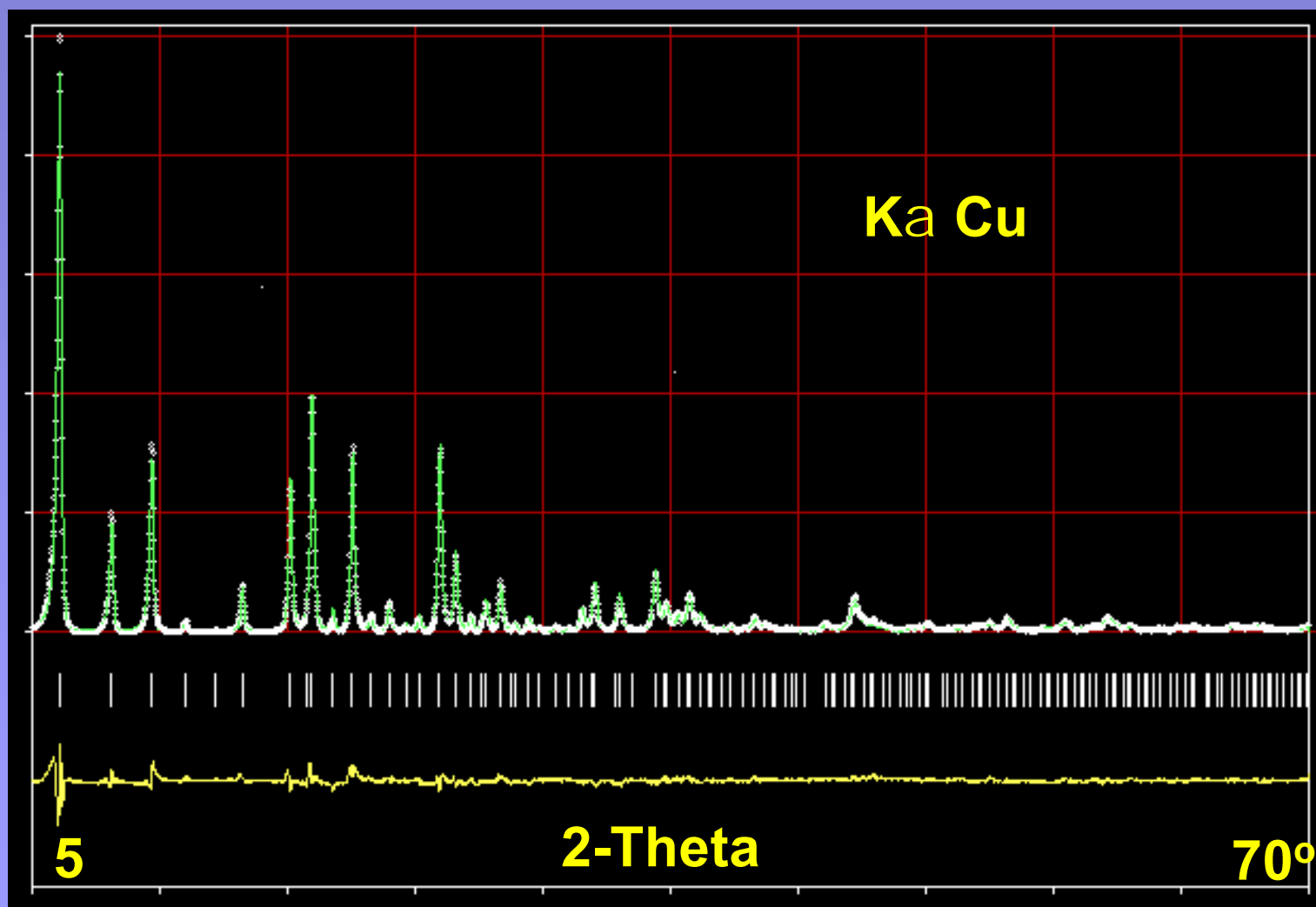
**MSPTOH: N-methyl-  
sparteinium hydroxide**





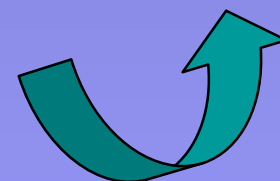
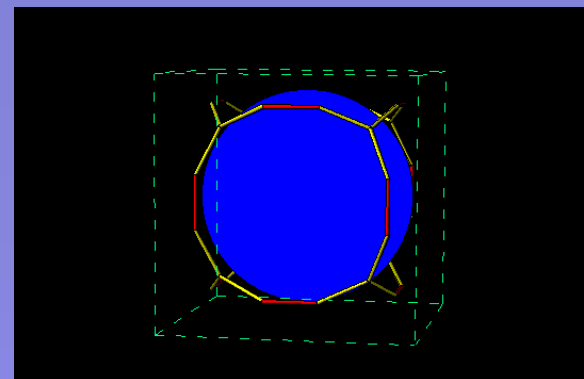
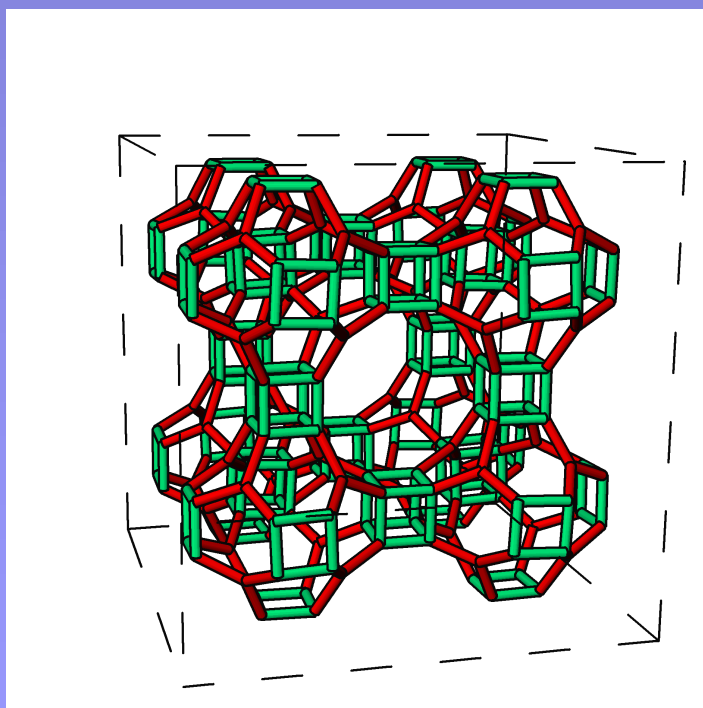


# X-ray powder diffraction pattern of ITQ-21





# Zeolite ITQ21 (as synthesised)



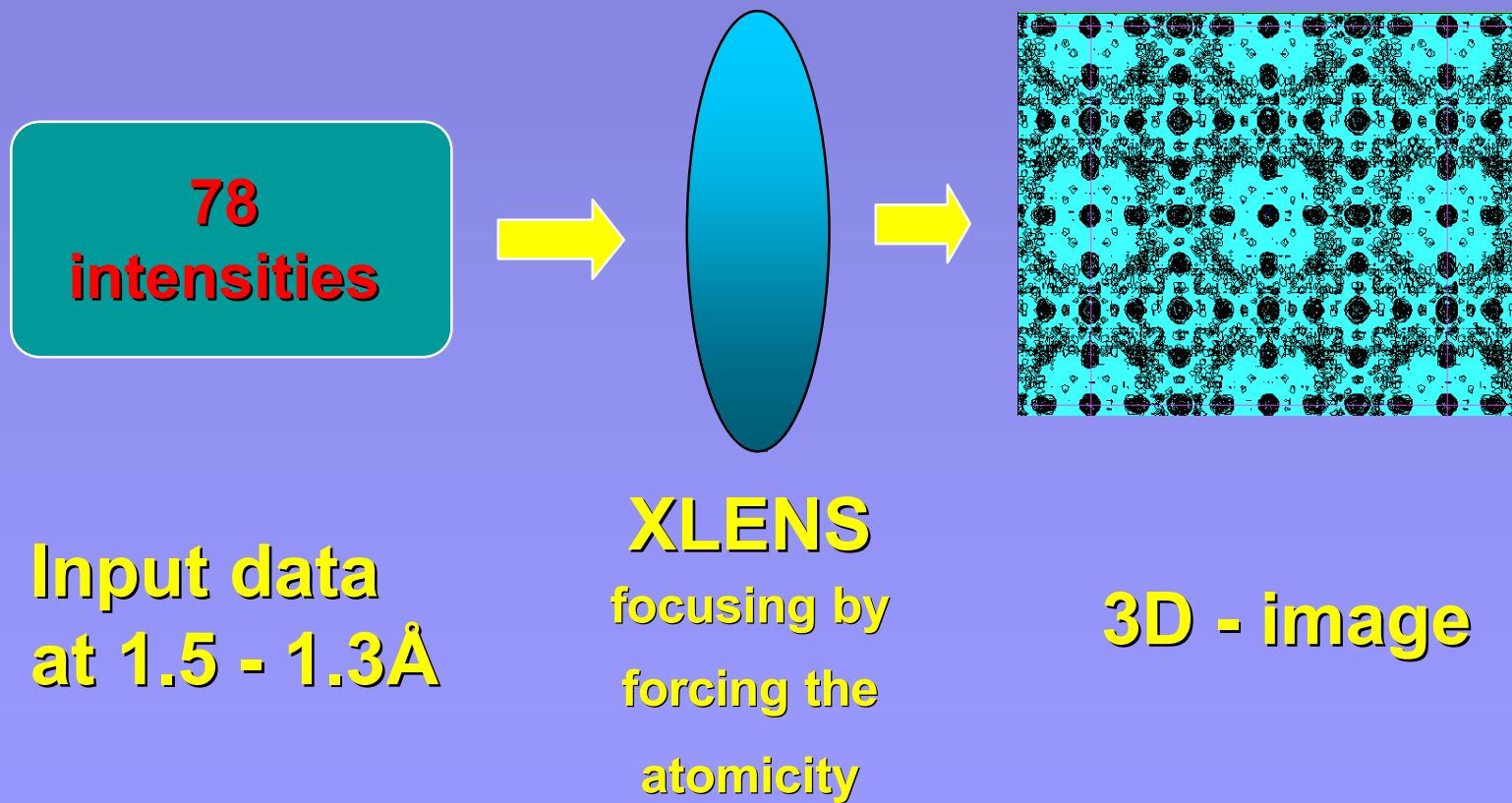
$$a = 27.70 \text{ \AA}$$

*Fm-3c*

A. Corma ... & J. Rius *Nature* (2002) 418, 514-517



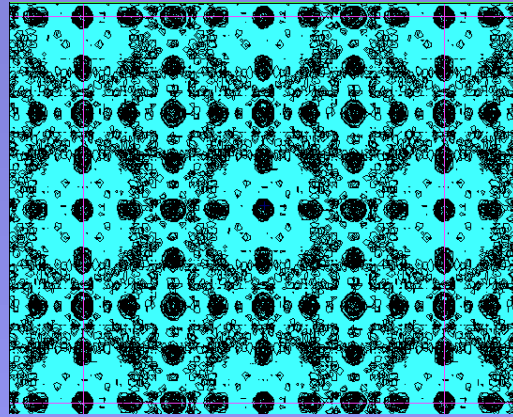
## 3D - imaging of ITQ-21 from moderate resolution X-ray data



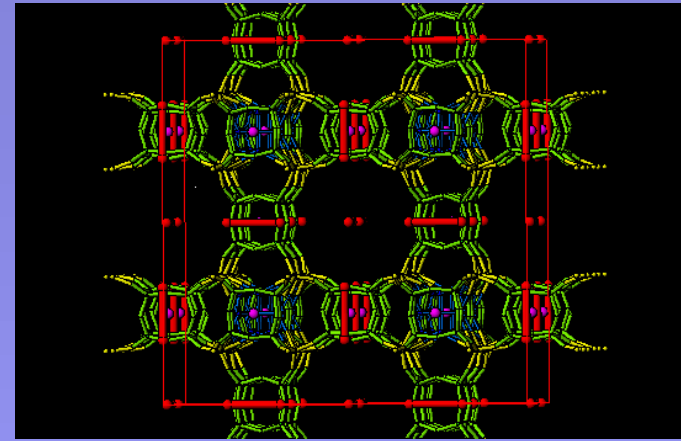
Rius, J. (1993) Acta Cryst. A49, 406-409



## Interpretation of the XRD image



at 1.5 Å

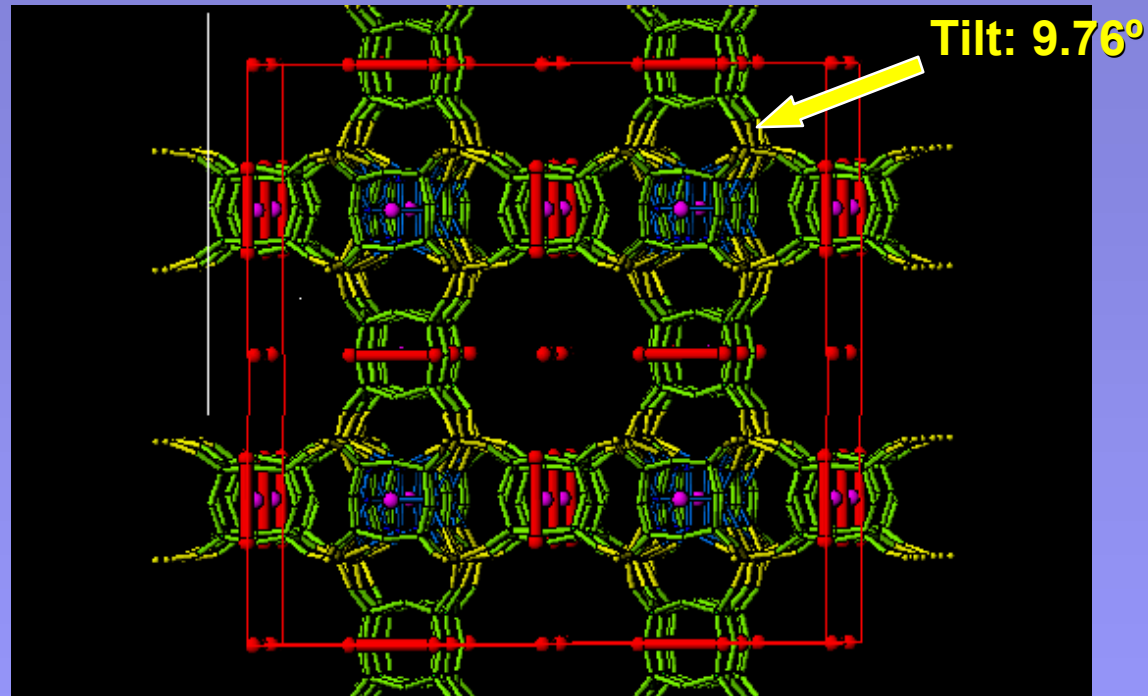


at atomic resolution

- ① What are the black peaks ?
- ① Why is the structure  $Fm-3c$  ?



## Why is the structure face-centered ?



Averaged structure:  $h=2n, k=2n, l=2n$  (strong)

Superstructure: Rest of reflections (weak)

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**Dr. Jose Luis Jordá**

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